

# The spatial effect of changes in regional characteristics

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# Overview

Introduction

The role of regional characteristics in location choice

The spatial and welfare effect of changes in regional characteristics

## Definition

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**properties** of geographical regions which may influence the residential **location choice** of households.

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Examples:

- city districts
- counties
- federal states
- nations (of a confederation such as the EU)

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Overall utility:

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↔ utility maximizing location choice **probabilities**:

$$\pi_{hr} = \frac{\exp(\lambda U_{hr})}{\sum_{r'} \exp(\lambda U_{hr'})}$$

## The deterministic utility

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Remarks:

- $Inc_{hr}$  denote per household income levels
- $pX_{hr}$  denote price indices
- The above formulation is usually called indirect utility function
- $q_{hr}$  denote inherent location attractiveness parameters  
↪ calibration

## Calibration of household location choice

Given:

- $\bar{Inc}_{hr}$  per household income levels (benchmark)
- $\bar{\pi}_{hr}$  household location choice probabilities (benchmark)
- $N_h$  number of households of type  $h$

Note:  $N_h \cdot \bar{\pi}_{hr}$  is the number of households of type  $h$  in region  $r$  in the benchmark.



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Wanted:

$$\pi_{hr} = \frac{\exp(\lambda U_{hr})}{\sum_{r'} \exp(\lambda U_{hr'})} = \frac{\exp(\lambda(\bar{Inc}_{hr} + q_{hr}))}{\sum_{r'} \exp(\lambda(\bar{Inc}_{hr'} + q_{hr'}))} \stackrel{!}{=} \bar{\pi}_{hr}$$

Since the income levels are given, only the parameters  $q_{hr}$  can be used to calibrate the location choice probabilities.

## Example

Let us assume the following:

- Only one household type, two regions  $R = \{1, 2\}$
- $\bar{lnc}_1 = 5.2$  and  $\bar{lnc}_2 = 3.7$
- Free parameter  $\lambda = 1$
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Problem: There is generally no unique solution!

Solution 1: Solution 3: ...

## Selecting unique parameter values

Unique parameter values are selected with the help of a constrained optimization procedure:

for all  $h$  :

$$\min \sum_r q_{hr}^2$$

$$\text{subject to } \bar{\pi}_{hr} = \frac{\exp(\lambda(\bar{l}nc_{hr} + q_{hr}))}{\sum_{r'} \exp(\lambda(\bar{l}nc_{hr'} + q_{hr'}))}$$

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Interpretation: Find, among all feasible values, those with the smallest sum of squares.

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Back to the example:

$$q_1 = -0.75 \text{ and } q_2 = 0.75.$$



## Explaining the location choice

The example gave  $q_1 = -0.75$  and  $q_2 = 0.75$ .

↔ There must be characteristics of region 2, apart from income, which cause a higher attractiveness for households to reside there (compared with region 1).

## Explaining the location choice

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↔ There must be characteristics of region 2, apart from income, which cause a higher attractiveness for households to reside there (compared with region 1).

Generally, a way to find out is to regress the  $q_{hr}$  on available regional characteristics  $g_{br}$ .

$$q_{hr} = \mu_h + \sum_{b \in B} \delta_{bh} \cdot g_{br} + \nu_{hr}$$

Note that:

- Other, possibly non-linear regression functions are allowed
- $|B| \ll |R|$  to obtain meaningful estimates

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- Here:  $\delta = \frac{q_1 - q_2}{g_1 - g_2} = 0.3$  and  $\mu = q_1 - \delta \cdot g_1 = -23.5$

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Now, it is possible to simulate how changes in  $g_r$  affect  $q_r$  and thus, the population distribution  $\pi_r$ .

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The evaluation criterion will be the following welfare function, which, technically, is the expected maximum utility (Anas/Xu, 1999):

$$W_h = \left( \sum_r \pi_{hr} \cdot U_{hr} \right) - \frac{1}{\lambda_h} \sum_r \pi_{hr} \cdot \ln \pi_{hr}$$

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## The direct welfare impact

Assume the regional characteristics take new values  $\tilde{g}_{br}$ .  
These affect the location attractiveness parameters:

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These affect the location attractiveness parameters:

$$\tilde{q}_{hr} = \mu_h + \sum_{b \in B} \delta_{bh} \cdot \tilde{g}_{br} + \nu_{hr},$$

Only the location choice probabilities are affected directly:

$$\tilde{\pi}_{hr} = \frac{\exp(\lambda(\text{Inc}_{hr} + \tilde{q}_{hr}))}{\sum_{r'} \exp(\lambda(\text{Inc}_{hr'} + \tilde{q}_{hr'}))}$$

The new welfare level containing the direct effect is:

$$\tilde{W}_h^{dir} = \left( \sum_r \tilde{\pi}_{hr} \cdot (\text{Inc}_{hr} + \tilde{q}_{hr}) \right) - \frac{1}{\lambda_h} \sum_r \tilde{\pi}_{hr} \cdot \ln \tilde{\pi}_{hr}$$

## Example: Direct welfare impact

Again the example:

Benchmark welfare level:

$$\begin{aligned}W^{bm} &= 0.5(5.2 - 0.75) + 0.5(3.7 + 0.75) - (0.5 \ln(0.5) + 0.5 \ln(0.5)) \\ &= 5.143\end{aligned}$$

Assume that the air quality index in region 2 drops by 1 point:

$$\tilde{g}_2 = g_2 - 1 = 79, \tilde{g}_1 = g_1 = 75:$$

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Assume that the air quality index in region 2 drops by 1 point:

$$\tilde{g}_2 = g_2 - 1 = 79, \quad \tilde{g}_1 = g_1 = 75:$$

$$\hookrightarrow \tilde{q}_2 = 0.45$$

$$\hookrightarrow \tilde{\pi}_2 = 0.426$$

$$\hookrightarrow \tilde{\pi}_1 = 0.574$$

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$$\hookrightarrow \tilde{\pi}_2 = 0.426$$

$$\hookrightarrow \tilde{\pi}_1 = 0.574$$

Counterfactual welfare level (only including the direct effect):

$$\begin{aligned} \tilde{W}^{dir} &= 0.574(5.2 - 0.75) + 0.426(3.7 + 0.45) - \\ &\quad (0.574 \ln(0.574) + 0.426 \ln(0.426)) \\ &= 5.004 \end{aligned}$$

## The total welfare impact

The total welfare impact consist of the direct and indirect impact:

The indirect impact includes changes of  $Inc_{hr}$  and  $pX_{hr}$  resulting from a **spatial shift** of economic activity.

This shift depends on how households interact with **other sectors** and how these sectors interact with each other.

In this multiregional model, **multiregional** I-O tables describe those interactions.



# Data basis

## Data basis: Interregional social accounting matrix (IRSAM)

		region 1					region 2				
		sector 1	sector 2	sector 3	sector 4	households	sector 1	sector 2	sector 3	sector 4	households
region 1	sector 1	0.6	0.4	0	0	1.6	0.2	0.2	0	0	0.8
	sector 2	0.2	0.5	0	0	1.6	0.1	0.3	0	0	1.2
	sector 3	1.1	1.6	0	0	0	0	0	0	0	0
	sector 4	1.5	1	0	0	0	0	0	0	0	0
	households	0	0	1.8	1.5	0	0	0	0.8	1.1	0
region 2	sector 1	0.3	0.2	0	0	0.8	0.3	0.1	0	0	0.5
	sector 2	0.1	0.2	0	0	1.2	0.1	0.8	0	0	1.2
	sector 3	0	0	0	0	0	0.6	1.5	0	0	0
	sector 4	0	0	0	0	0	0.9	0.7	0	0	0
	households	0	0	0.9	1	0	0	0	1.3	0.5	0

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Method to derive intraregional I-O relations (FLQ formula) and interregional I-O relations (gravity model) from national tables:

Jahn, M. (2016): Extending the FLQ Formula: A Location Quotient-based Interregional Input-Output Framework, *Regional Studies*, doi: 10.1080/00343404.2016.1198471.

## The aggregate model (1)

The household expenditure from the IRSAM is used to calibrate a CES utility function:

$$U_{hr} = A_{hr} \left( \sum_{m \in M, s \in R} \beta_{mhsr} \cdot C_{mhsr}^{\rho_h} \right)^{1/\rho_h}$$

with

- $A_{hr}$  ( $A_{hr} > 0$ ) scale parameter
- $C_{mhsr}$  quantities demanded by a household of type  $h$  located in region  $r$  from final sector  $m$  ( $m \in M$ ) in region  $s$ .

Interpretation  $C_{m \rightarrow h}^{s \rightarrow r}$

- $\beta_{mhsr}$  ( $\beta_{mhsr} \geq 0$ ;  $\sum_{m,s} \beta_{mhsr} = 1$ ) share parameters
- $\rho_h$  ( $-\infty < \rho_h < 1$ ) elasticity of substitution parameter

Note that the CES function can be written as  $U_{hr} = Inc_{hr}/p_{X_{hr}}$ .

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Other supply and demand functions can be calibrated from the IRSAM:

- Factor supply functions of households
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The location choice is included in the **general equilibrium** through the market clearing equations (here for primary factors  $f \in F$  in region  $r$ ):

$$\sum_{h \in H, s \in R} N_h \cdot \pi_{hs} \cdot S_{hfsr} = \sum_{m \in M, s \in R} Y_{fmsr}$$

Interpretation of the individual household supply:  $S_{h \rightarrow f}^{s \rightarrow r}$

Interpretation of the primary input demands:  $Y_{f \rightarrow m}^{r \rightarrow s}$

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- Monetized total welfare impact: 2.956 billion €
- Thereof direct welfare impact: 2.776 billion €

## Summary

Usefulness of the model:

- In general: Assessment of household relocation effects of any type of shock/policy



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## Extensions:

- Household types  $h = \{s, r\}$ , i.e. simultaneous choice of zone of residence and zone of work ( $\rightarrow$  commuting)
- Introduce sectoral emissions intensities and their effect on air quality ( $\rightarrow$  regional integrated assessment model)
- Introduce time  $t$  ( $\rightarrow$  e.g. long-term impacts of climate change)

# The spatial effect of changes in regional characteristics

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